

Microstructure and fracture toughness of a spark plasma sintered Al_2O_3 -based composite with BaTiO_3 particulates

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Abstract

Dense Al_2O_3 -based composites with dispersed BaTiO_3 particulates were fabricated by using spark plasma sintering (SPS) at sintering temperatures between 1100 and 1500 °C with a heating rate of 100 °C/min. High-density of BaTiO_3 - Al_2O_3 with various compositions could be achieved by SPS at lower sintering temperatures compared to those by conventional pressure-less sintering (PLS). However, full densification was prevented by the onset of abnormal grain growth in Al_2O_3 - BaTiO_3 composites sintered by SPS. It was found that SPS process could accelerate the abnormal grain growth due to the activation and purification of particle surface. The addition of BaTiO_3 in Al_2O_3 matrix improved fracture toughness of the composites fabricated by both SPS and PLS. The highest fracture toughness of 6.04 $\text{MPa}\cdot\text{m}^{1/2}$ was achieved in the composite sintered by SPS process with 5 mol% BaTiO_3 , while that of the monolithic Al_2O_3 was about 4.0 $\text{MPa}\cdot\text{m}^{1/2}$.

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1. Introduction

Since ceramic materials have various advantages to demonstrate their functions, there are many potential applications. However, ceramics are brittle and show catastrophic fracture. The objective of many researches concerned with structural ceramics is the development of materials with high reliability. The toughening approach attempts to create microstructures that result in sufficient fracture resistance. In addition, intelligent materials with self-sensing function, self-effecting function, etc. have been widely studied.¹

The ferroelectric material has an interesting mechanical–electrical coupling properties.^{2,3} The electric fields can influence the fracture toughness of ferroelectric material. For example, polarized ferroelectrics exhibit anisotropic fracture toughness. The material is tougher for a crack parallel to the poling direction but less tough for a crack perpendicular to it.² When an electric field is applied to polarized ferroelectrics, a positive field

reduces its fracture toughness but a negative field enhances it. In the past few years, Niihara and his colleagues have proposed ferroelectric-based nanocomposites with high strength and toughness, such as PZT/Pt,⁴ $\text{BaTiO}_3/\text{MgO}$ ⁵ and $\text{BaTiO}_3/\text{SiC}$.⁶ Many researchers have extensively investigated their excellent mechanical properties and also electrical properties such as dielectric constant and the Curie temperature. Since the strain change due to the electro-magnetic field is a physical reaction, piezoelectric-particle-dispersed ceramics would have an advantage that strain sensing function can be directly obtained through measuring the electric field. Chen and his colleagues have proposed a novel approach to toughening of ceramics, where piezoelectric secondary phases were introduced into the matrix such as $\text{BaTiO}_3/\text{Al}_2\text{O}_3$,⁷ $\text{BaTiO}_3/3\text{Y-TZP}$,⁸ $\text{Nd}_2\text{Ti}_2\text{O}_7/\text{Al}_2\text{O}_3$,⁹ $\text{Sr}_2\text{Nb}_2\text{O}_7/3\text{Y-TZP}$ ¹⁰ and $\text{BaTiO}_3/\text{ZrO}_2$,¹¹ and the energy dissipation due to the piezoelectric effect and domain wall's motion was suggested as the main toughening mechanism.

Spark plasma sintering (SPS) is one of the solid consolidation processes and is carried out in a graphite mold but the heating is accomplished by spark discharges in voids between particles.¹² SPS has the

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combination of pulsed electrical discharge with rapid heating and pressure application to achieve fast sintering of powders. Takeuchi et al.¹³ fabricated dense barium titanate ceramics (97% relative density) with submicrometer-sized grains by SPS, where the grain size is about 0.6 μm and almost the same as that of starting powders. They also produced dense PbTiO_3 ceramics with submicrometer-sized grains by the SPS process.¹⁴

In the present work, ferroelectric BaTiO_3 dispersed Al_2O_3 ceramics were sintered by SPS as well as conventional pressure less sintering (PLS). Toughening effect of the composite was investigated together with the microstructural characterization.

2. Experimental procedure

2.1. Materials and sintering procedure

Commercial BaTiO_3 powders (BT-05, Sakai chemical industrial Co. Ltd.) with an average particle size of 0.5 μm and high purity Al_2O_3 powders (Sumitomo Sekitan Kougyo, KK) with an average particle size of 0.2 μm were used as the starting materials. Compositions of these powders are shown in Table 1.

The $x \text{ BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composite powders ($x=0.01, 0.03, 0.05$ and 0.10) were mixed by a ball milling machine with alumina balls in ethanol for 24 h. The wet slurry was then dried by using a rotary evaporator. Dried powders were milled again and sieved through a 150- μm mesh screen. The mixed granules were put into a graphite die with diameter of 25 mm which was on the vibration table for homogeneous packing of the powders and then were sintered using a spark plasma sintering machine by heating at sintering temperatures between 1100 and 1500 $^\circ\text{C}$ under a pressure of 38 MPa at a heating rate of 100 $^\circ\text{C}/\text{min}$ in vacuum. The soaking time at the sintering temperature was 3–5 min and cooling time from the sintering temperature to 600 $^\circ\text{C}$ was about 30 min. The temperature was measured by means of an optical pyrometer focused on the graphite die surface.

A conventional PLS of the composite powders was also conducted for comparison. The mixed granules with PVA binder were formed into rectangular bars by

uniaxially pressing and then compacted by cold isostatic pressing (CIP) at 200 MPa. The compacts were fired in a furnace at temperatures ranged from 1300 to 1450 $^\circ\text{C}$ for 2 h in air at a heating rate of 10 $^\circ\text{C}/\text{min}$. Dimensions of the bar were 15 mm in width, 15 mm in height and 80 mm in length. The monolithic alumina was also prepared by the same sintering methods.

2.2. Characterization

The bulk density was determined by Archimedes' method in water. The X-ray diffraction (XRD) analysis was conducted using Shimadzu XRD 6100 with nickel-filtered $\text{Cu } K_\alpha$ radiation. The average grain size and pore size of the samples were determined from scanning electron micrographs on the polished and etched surfaces.

2.3. Fracture toughness testing

Fracture toughness was evaluated by the indentation fracture (IF) method with the equation proposed by Niihara et al.¹⁵ Indentation racks were induced at a load of 98 N for 15 s using a Vickers hardness tester. The indentation crack path was observed by using a scanning electron microscope (SEM) in detail.

3. Results and discussion

3.1. XRD analysis

From the results of XRD analysis, some intermediate phases such as $\text{BaAl}_{13.2}\text{O}_{20.8}$ and $\text{BaAl}_6\text{TiO}_{12}$ as well as BaTiO_3 and Al_2O_3 phases were found, as shown in Fig. 1. Relative X-ray peak intensities of these phases are listed in Table 2. Because of reaction between BaTiO_3 and Al_2O_3 , the BaTiO_3 secondary phase was significantly reduced. The peak angles of BaTiO_3 and $\text{BaAl}_{13.2}\text{O}_{20.8}$ are almost identical. It is then difficult to distinguish the two phases. In the figure, the intensity of $\text{BaAl}_{13.2}\text{O}_{20.8}$ includes that of BaTiO_3 . The total amount of the intermediate phases increased with increasing the amount of BaTiO_3 addition and sintering temperature.

Table 1
Characterization of barium titanate powder (BT-05) and alumina powder

	$\alpha\text{-Al}_2\text{O}_3$	Si	Fe	Na	K	Ca	Mg	BET analysis (m^2/g)	Ave. particle size (μm)
Al_2O_3 powder	99.99%	6 ppm	7 ppm	3 ppm	1 ppm	1 ppm	1 ppm	12.9	0.20
	Ba/Ti ratio	SrO (wt%)	CaO	Na_2O	SiO_2	Al_2O_3	Fe_2O_3		
BaTiO_3 powder	1.00	0.01	<0.001	0.001	0.001	<0.001	0.001	2.4	0.5

3.2. Microstructure

Figs. 2 and 3 show microstructures of monolithic alumina and BaTiO₃-Al₂O₃ composites sintered at 1200 and 1300 °C by SPS, respectively. Al₂O₃, intermediate and BaTiO₃ grains in the SEM micrographs (Back scattering electrons image) are black, gray and white regions, respectively. From Fig. 2, it is seen that the samples with 3 and 5 mol% BaTiO₃ were not well sintered at 1200°, where isolated powders were observed, while the sample with 10 mol% BaTiO₃ was well sintered. It is seen from Fig. 3 that the samples were well sintered at 1300 °C. For the sintering temperatures

lower than 1200° and higher than 1300 °C, the samples were crashed and/or cracked during the sintering process. It is also found that the BaTiO₃ phase was not uniformly distributed in the Al₂O₃ matrix phase. Fig. 4 shows microstructures of monolithic alumina and BaTiO₃-Al₂O₃ composites sintered by PLS. It can be seen from the figure that there are lots of small pores. For the sintering temperatures lower than 1400 °C, it seemed that dense samples could not be obtained.

Average grain size of monolithic alumina sintered by SPS was approximately 1–2 μm with larger grain sizes up to 4 μm, while that by PLS was about 8 μm. Smaller grain size can be obtained by SPS compared to conventional

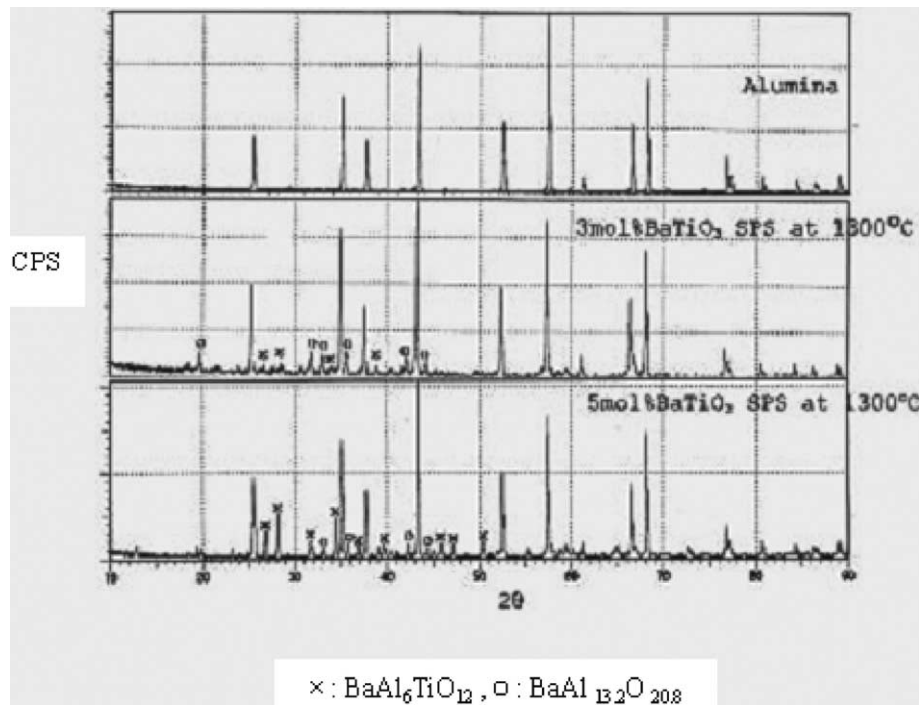


Fig. 1. X-ray diffraction patterns of x BaTiO₃/(1- x) Al₂O₃ composites with $x=0, 0.03$ and 0.05 sintered by SPS at 1300 °C.

Table 2
Characterization of sintered composites

Sintering method	Sintering temp. (°C)	%mol BaTiO ₃	Relative X-ray peak intensity of phases analysis			Average alumina matrix grain size (μm)
			I _{BATO} /I _{Al₂O₃}	I _{BAO} /I _{Al₂O₃}	Total of I _{BATO} + I _{BAO}	
PLS	1400	3	0.051	0.045	0.096	5.84
		5	0.186	0.063	0.249	3.8
	1450	3	0.139	0.050	0.189	6.6
		5	0.288	0.081	0.369	4.2
SPS	1200	3	0.034	0.049	0.083	0.50
		5	0.076	0.063	0.139	0.53
	1300	3	0.038	0.108	0.146	0.6/6.406
		5	0.118	0.086	0.204	0.625/6.80

Abbreviation: BATO:BaAl₆TiO₁₂, BAO:BaAl_{13.2}O_{20.8}.

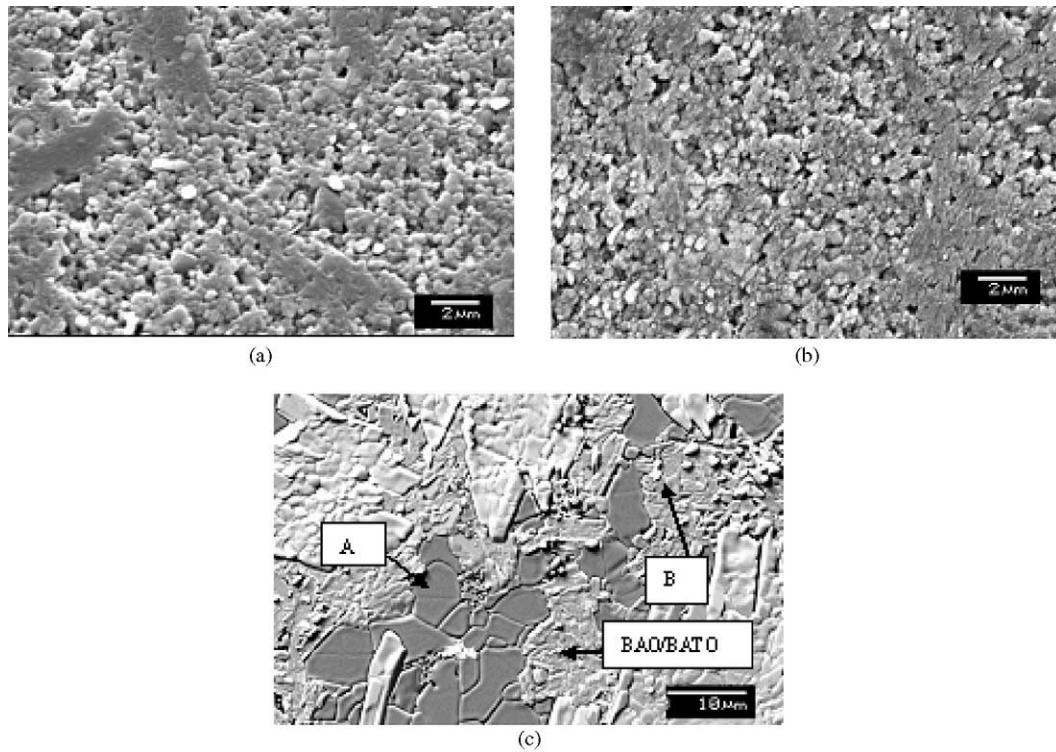


Fig. 2. Scanning electron micrographs of thermal etched surface of $x\text{BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composites sintered by SPS (a) $x=0.03$, (b) $x=0.05$ and (c) $x=0.10$ at $1200\text{ }^\circ\text{C}$. A: Al_2O_3 phase, B: BaTiO_3 phase and BAO/BATO: intermediate phase.

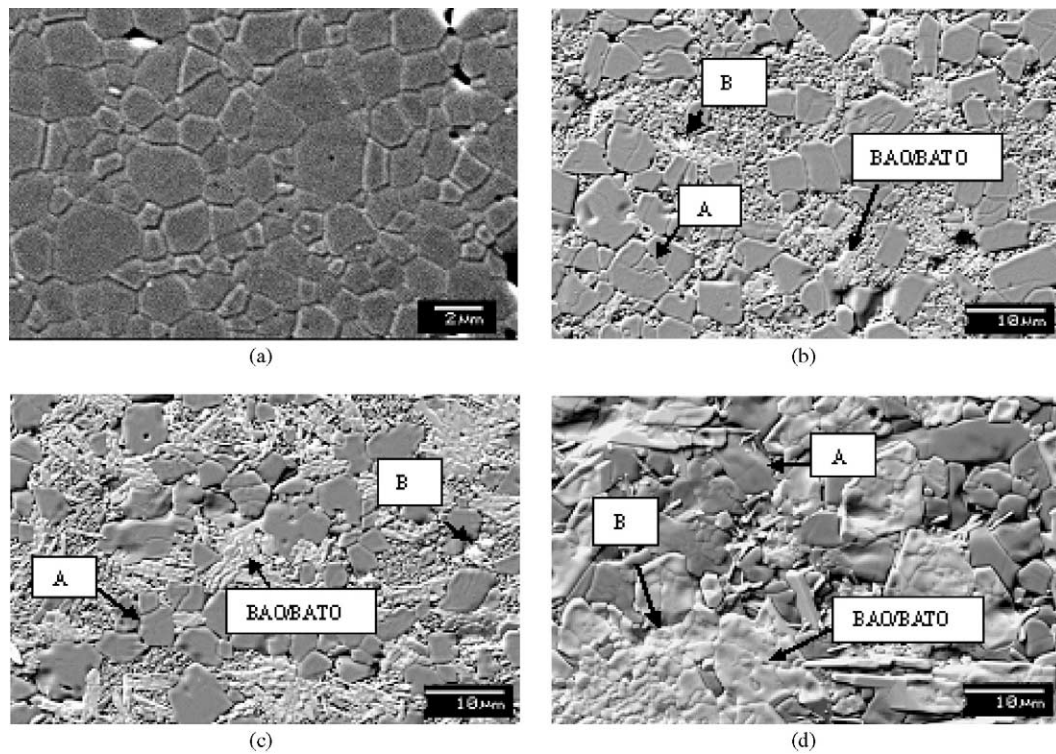


Fig. 3. Scanning electron micrographs of thermal etched surface of $x\text{BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composites sintered by SPS (a) $x=0$, (b) $x=0.01$, (c) $x=0.03$, (d) $x=0.05$ at $1300\text{ }^\circ\text{C}$. A: Al_2O_3 phase, B: BaTiO_3 phase and BAO/BATO: intermediate phase.

PLS. Average alumina grain sizes of $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites are listed in Table 2. The average alumina grain sizes of the composites sintered by SPS were significantly small compared to those by PLS by a factor of 10. The grain sizes increased with increasing sintering temperature.

The microstructures of composites with 3 and 5 mol% BaTiO_3 sintered by SPS at 1300 °C were bimodal with large grains in fine-grain matrix, as shown in Fig. 3(b), (c) and (d). The size of large grain of the SPS composites increased dramatically with increasing BaTiO_3 content. The large grains grew longitudinally to plate-like shape. Large plate-like grains, which have grown at the expense of small ones, may represent coarsening under the presence of liquid phase. From BaO-TiO_2 system,¹⁶ BaTiO_3 can form liquid phase at 1322 °C. This result suggests that small amount of BaTiO_3

addition to Al_2O_3 leads to liquid phase being formed at the grain boundaries, which enhances surface diffusion and hence grain growth.

From Fig. 3, large pores were observed at grain boundaries and the grain size was almost the same regardless of BaTiO_3 content. Fig. 3 also shows the agglomerated BaTiO_3 grains and suggests the aggregated of intermediate phase being formed at grain boundaries. Thus, the addition of BaTiO_3 is deleterious for the fabrication of dense $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites with fine grains.

3.3. Density

Relationships between relative density and sintering temperature for $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites sintered by SPS and PLS are shown in Fig. 5. It can be seen from

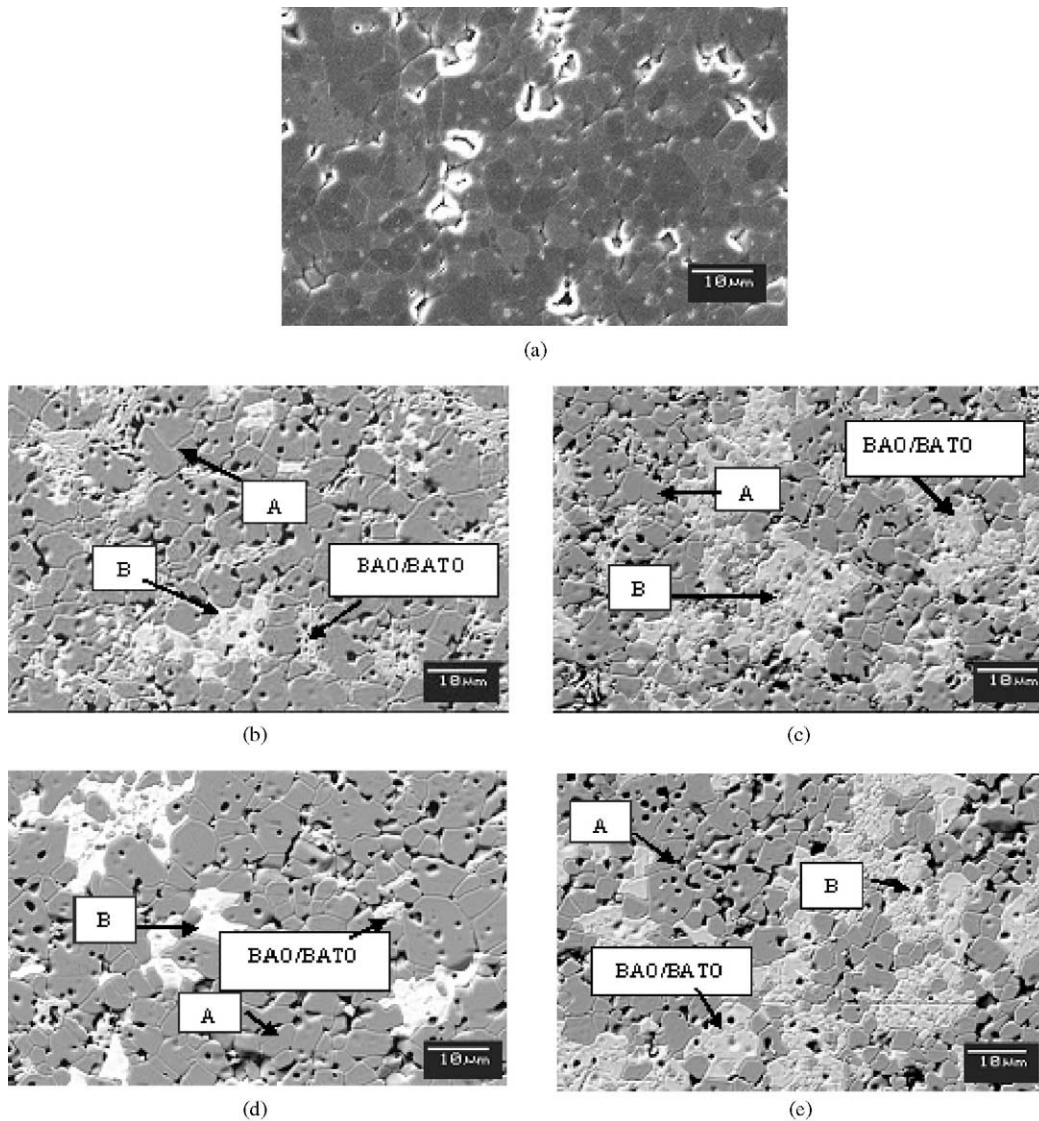


Fig. 4. Scanning electron micrographs of thermal etched surface of $x\text{BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composites sintered by PLS (a) $x=0$, (b) $x=0.03$, (c) $x=0.05$ at 1400 °C and (d) $x=0.03$, (e) $x=0.05$ at 1450 °C. A: Al_2O_3 phase, B: BaTiO_3 phase and BAO/BATO: intermediate phase.

the figure that the relative density increased with increasing sintering temperature. Higher relative density of the composites could be obtained by SPS compared to PLS. Fig. 6 shows relationship between density of $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites and BaTiO_3 content. As can be seen from the figure, density decreased with increasing BaTiO_3 content for both SPS and PLS methods. The highest densification of SPS samples was attained in the $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composite sintered at $1300\text{ }^\circ\text{C}$, while it was not successful to densify at sintering temperatures above $1300\text{ }^\circ\text{C}$. Since the temperature inside the graphite die is higher than the temperature measured on the surface of die by about $100\text{--}200\text{ }^\circ\text{C}$, process-induced flaws might be caused by the hexagonal-cubic transition of BaTiO_3 (at $1460\text{ }^\circ\text{C}$) associated with the high cooling rate of SPS system. Furthermore, the composites with addition of BaTiO_3 indicated lower density than monolithic Al_2O_3 .

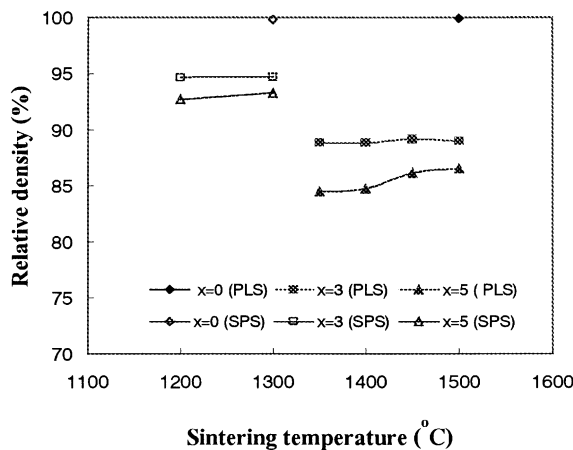


Fig. 5. Relationship between sintering temperature and relative density of $x\text{BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composite sintered by SPS and PLS.

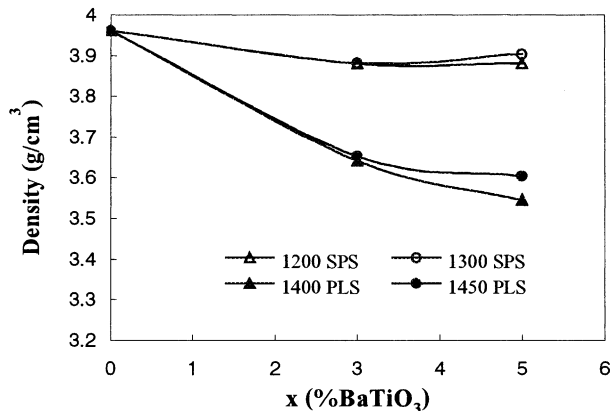


Fig. 6. Relationship between density of $x\text{BaTiO}_3/(1-x)\text{Al}_2\text{O}_3$ composite and BaTiO_3 content.

3.4. Hardness

Fig. 7 shows relationship between Vickers hardness and BaTiO_3 content for the composites sintered by SPS and PLS. The hardness decreased with increasing BaTiO_3 content and sintering temperature. SPS produced higher hardness materials compared to PLS. This may be caused by the finer grains as well as higher density of SPS composites.¹⁷

3.5. Fracture toughness

Fig. 8 shows relationship between fracture toughness K_{IC} and BaTiO_3 content. The scatter bands of the data are also indicated in the figure, while they are rather large. From the figure, fracture toughness of the $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composite sintered at $1300\text{ }^\circ\text{C}$ by SPS was significantly improved with increasing the amount of BaTiO_3 addition up to 5 mol%. The maximum fracture toughness of $6.04\text{ MPa}\cdot\text{m}^{1/2}$ was obtained for the composition of $\sim 5\text{ BaTiO}_3/95\text{ Al}_2\text{O}_3$, while the fracture

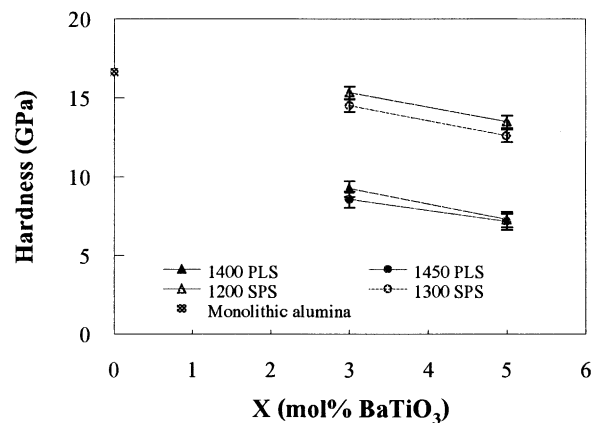


Fig. 7. Vickers hardness vs. BaTiO_3 content for $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites sintered by SPS and PLS.

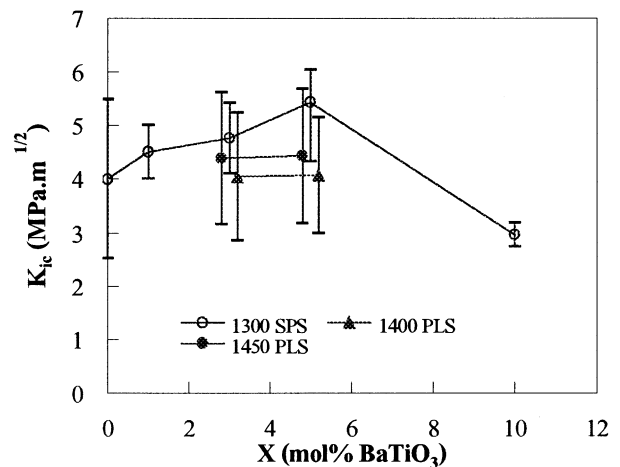


Fig. 8. Fracture toughness vs. BaTiO_3 content for $\text{BaTiO}_3\text{-Al}_2\text{O}_3$ composites sintered by SPS and PLS.

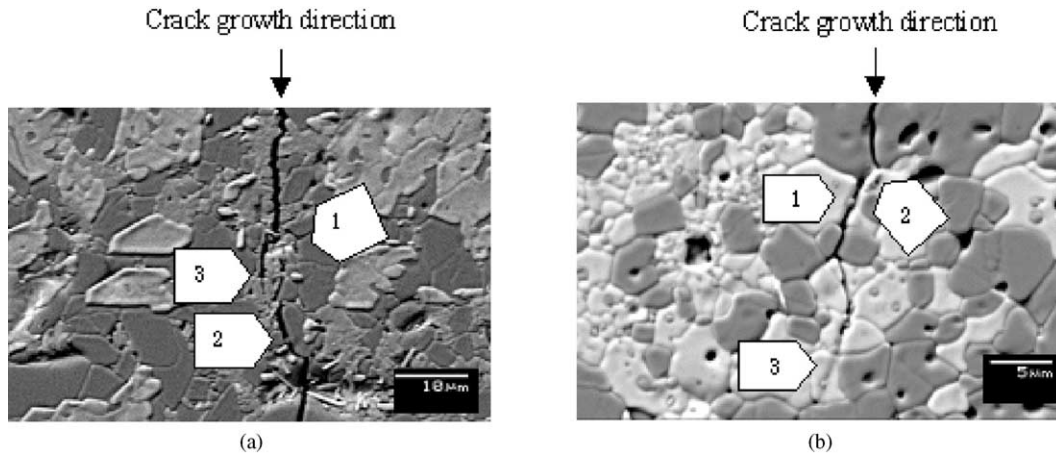


Fig. 9. Indentation cracks on polished surface of (a) 5 mol% BaTiO₃-SPS composite at 1300 °C and (b) 3 mol% BaTiO₃-PLS composite at 1450 °C. The white arrows are indicated as: 1 = deflection at or near BaTiO₃ particles, 2 = crack bridging, 3 = crack arresting at or in the intermediate phases.

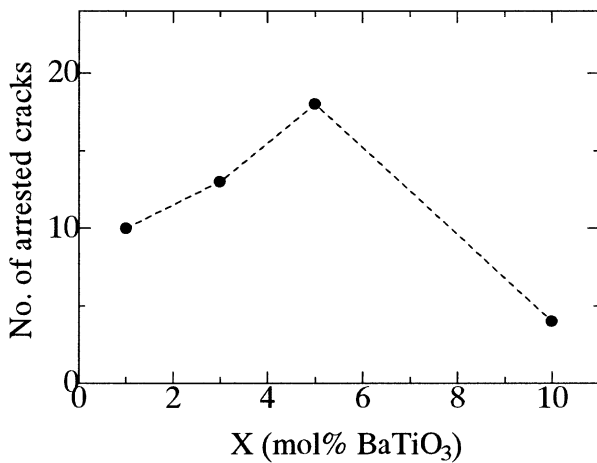


Fig. 10. The numbers of arrested indentation cracks at intermediate phases as function of BaTiO₃ content.

toughness of monolithic Al₂O₃ was about 4 MPa.m^{1/2}. When the content of BaTiO₃ increased up to 10 mol%, fracture toughness of the composite sintered at 1300 °C by SPS was significantly reduced. Fracture toughnesses of the BaTiO₃-Al₂O₃ composites sintered by PLS were equal to or higher than that of monolithic Al₂O₃.

Fig. 9 shows examples of the crack paths for the fracture toughness test specimens. It can be seen from the figure that there are three typical features of the crack path: (1) crack deflection at or near BaTiO₃ particles, (2) crack bridging, and (3) crack arresting at or in the intermediate phases. The crack bridging and arresting at or in the intermediate phases were often observed on the crack wake, as shown in the figure. Fig. 10 shows the number of arrested cracks at or in the intermediate phase as a function of amount of BaTiO₃ addition for the samples sintered by SPS at 1300 °C. In the figure, the total number of observed cracks was 24 for each sample. It can be seen from the figure that the number

of arrested cracks increased with increasing the BaTiO₃ content up to the amount of 5 mol% and then decreased. This tendency agrees well with that of fracture toughness shown in Fig. 8, which suggests higher toughness of the intermediate phases compared to that of Al₂O₃ matrix. It is well known that crack bridging significantly reduces the crack tip stresses and then enhances the crack growth resistance.¹⁸ Therefore, the intermediate phases will significantly contribute the higher fracture toughness. The crack deflection at or near BaTiO₃ particles was also observed. It is also known that ferroelectric phases will induce compressive stress around them during loading process due to stress-induced domain switching and then contribute the improvement of fracture toughness.^{7,19–22} In an unpolarized piezoelectric domain switching is also possible if those domains are in a suitable orientation. However, since the BaTiO₃ phase easily reacted with the Al₂O₃ phase and the intermediate phases were produced, the only small amount of BaTiO₃ phase remained in the samples. Therefore, the effect of BaTiO₃ phase on fracture toughness of the present samples may not be dominant, while the phase will have some effect on toughness in its nature.

4. Conclusion

Piezoelectric secondary phase dispersed ceramic composites, BaTiO₃-Al₂O₃, could be produced by the SPS method and densified composites could be obtained in contrast to that by the PLS method. The highest densification of SPS samples (95% relative theoretical density) was attained in BaTiO₃-Al₂O₃ ceramics at the sintering temperature of 1300 °C by SPS, while the densification was not successful at sintering temperatures above 1300 °C. The relative density of sintered SPS

composites was higher than that of sintered PLS composites. The relative density of BaTiO₃-Al₂O₃ composites was decreased with increasing BaTiO₃ content. The microstructure of sintered SPS composites indicated fine alumina grains with some abnormal grain growth of intermediate phases. The abnormal grain growth could be caused by the spark discharge happened between the particles, which increased the surface activity of the powder and then accelerated the surface diffusion. However, the fracture toughness of the BaTiO₃-Al₂O₃ composites was improved and the highest fracture toughness of 6.04 MPa.m^{1/2} for the Al₂O₃ with 5 mol% BaTiO₃ sintered by SPS at 1300 °C was achieved.

Crack bridging and crack arresting at or in the intermediate phases were increasingly observed in the higher toughness samples, which indicates that the intermediate phases must contribute to the higher fracture toughness. The crack deflection at or near BaTiO₃ particles was also observed. However, only small amount of BaTiO₃ phase remained in the present composites and then the contribution to higher fracture toughness will be not significant. If large amount of BaTiO₃ phase could be remained in the composite, fracture toughness will be improved further, which will be the next work.

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